



Performance, accuracy and bit-reproducibility aspects in handling transcendental functions with Cray and Intel compilers for the Met Office Unified Model

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Some requirements for meteorological applications

- Performance
 - vectorisation
 - human factor: time spent to achieve a certain level in the performance gain
- >Accuracy
 - single & double precision in weather forecasting models
- Results bit-reproducibility

Note: all above mentioned aspects are applied for handling transcendental functions in an application and will be discussed in the presentation



Vector processing: Fortran compiler options related to the architecture

>Intel compiler: -xcode for specific processor architecture

- AVX Intel Xeon processor E3/E5 and E3/E5/E7 v2 family
- CORE-AVX2 Intel Xeon processor E3/E5/E7 v3, v4 family
- CORE-AVX512 Intel Xeon Processor Scalable Family
- Host architecture on which the code is compiled

Cray compiler: -h cpu=target_system

Compiler options set via modules on our XC-40 systems are

Module	Cray compiler	Intel compiler
craype-sandybridge	-hcpu=sandybridge	-mavx
craype-haswell	-hcpu=haswell	-xCORE-AVX2
craype-broadwell	-hcpu=broadwell	-xCORE-AVX2



Results bit-reproducibility

> Means getting identical results on a job rerun

Benefits: useful in testing, debugging, tracking down code bugs or numerical instability

Numerical implementation of UM includes a setting which provides results bit-reproducibility using different number of threads for the same horizontal decomposition



Rerun bit-reproducibility

>Intel Fortran compiler => need to specify

- -fp-model precise
- may effect vectorisation of loops for some transcendental functions called within the loops

Note: below

- any reference to a compiler means Fortran compiler
- -fp-model precise is used in the Intel compiler case
- Cray compiler : results bit-reproducibility may depend on -h flex_mp=level



Accuracy in calculation of transcendental functions

Accuracy is measured in terms of ULP

(unit in the last place or unit of least precision)

 accuracy for Cray CCE math libraries is controlled by -hfpN option

Intel compiler		Cray compiler		
default	-fp-model precise	-hfp0 -hfp1 -hfp2	-hfp3	-hfp4
4 ULP	0.6 ULP	1.3 ULP	2.6 ULP	4 ULP

Note: -hfp4 is used to compile the majority of UM files



Vectorisation information for some transcendental functions in loops

With the Cray compiler and the Intel compiler with -fp-model precise, loops are

- vectorised with SQRT, SIN, COS, EXP
- NOT vectorised with ASIN, ACOS, ATAN

	Power (x^y)	ALOG	ALOG10	TANH	ATAN2
Cray compiler	Yes	Yes	No	No	Yes
Intel compiler	No	No	No	Yes	No



Can loops for all transcendental functions be vectorised?

- Cray compiler: NO (as far as I know)
- > Intel compiler: YES in two ways
 - -fast-transcendentals -fimf-precision=<value>

```
<value> = high | medium | low
high - 1 ULP, used in this presentation
medium - 4 ULP, also tested with very similar performance
low - not used
```

 Intel Math Kernel Library (MKL) library using vector math library (the error usually is <0.75 ULP with high accuracy)



Environment for implementation

Hardware

Cray XC-40 (Terra), Intel Xeon E5-2690 v3, 2.6 GHz
 136 nodes with 24 cores/node (3264 cores)

Software

- Intel compiler v17.0.1.132
- Cray cce 8.4.5
- Cray MPICH 7.3.2
- MPI_WTIME for time measurements



UM job description

- > UM10.7 sources (Feb 2017)
- > N768L70 (1532x1152x70 grid size) global model
- > 24 hour (192 time steps) forecast with switched off I/O to tune computational capability of the model sources
- run configuration: 16x30 horizontal decomposition with 2 threads on 960 cores
 - elapsed time for the job is 920-950 sec

Note: the job was used within the OpenMP coverage improvement collaboration project with the Met Office for UM10.4-10.8 releases



Example: departure_point_eta_mod.F90

Subroutine includes 8 three-level nested loops:

251	DO $k = 1$, model_levels
252	DO j = udims%j_start, udims%j_end
253	DO i = udims%i_start, udims%i_end
• •	•
276	$z_d = SQRT(1.0 - x_d**2 - y_d**2)$
277	
278	<pre>depart_xi1(i,j,k) = xi1_u(i) + &</pre>
279	<pre>ATAN2(x_d,z_d*csxi2_p(j)-y_d*snxi2_p(j))</pre>
280	<pre>depart_xi2(i,j,k) = ASIN(y_d*csxi2_p(j)+z_d*snxi2_p(j))</pre>
281	<pre>depart_xi3(i,j,k) = eta_rho_levels(k) - timestep*w_a</pre>
282	END DO
283	END DO
284	END DO



Cray compiler loopmark output for the loop

Loopmark output with -rm compiler option

251.	+ M m<	DO $k = 1$, model_levels	
252.	+ M m 3<	DO j = udims%j_start, udims%j_end	
253.	M m 3 Vp<	DO i = udims%i_start, udims%i_end	
• • •			
276.	Mm 3 Vp	$z_d = SQRT(1.0 - x_d**2 - y_d**2)$	
277.	Mm 3 Vp		
278.	Mm 3 Vp	<pre>depart_xi1(i,j,k) = xi1_u(i) +</pre>	&
279.	Mm 3 Vp	$ATAN2(x_d,z_d*csxi2_p(j)-y_d*snxi2_p(j))$	
280.	Mm 3 Vp	<pre>depart_xi2(i,j,k) = ASIN(y_d*csxi2_p(j)+z_d*snxi2_p(j))</pre>	
281.	Mm 3 Vp	<pre>depart_xi3(i,j,k) = eta_rho_levels(k) - timestep*w_a</pre>	
282.	M m 3 Vp>	END DO	
283.	M m 3>	END DO	
284.	M m>	END DO	

A loop starting at line 253 was partially vectorized.

Comments:

- the inner loop is only partially vectorised
- the loopmark output does not provide details on what is not vectorised



Intel compiler diagnostic for the loop

-fp-model precise -qopt-report=5 -qopt-report-phase=vec

LOOP BEGIN at <path>/departure_point_eta_mod.F90(253,9) remark #15382: vectorization support: call to function atan2 cannot be vectorized [<path>/departure_point_eta_mod.F90(279,31)] remark #15382: vectorization support: call to function asin cannot be vectorized [<path>/departure_point_eta_mod.F90(280,31)] remark #15344: loop was not vectorized: vector dependence prevents vectorization LOOP END

-fp-model precise -fast-transcendentals -fimf-precision=high -qopt-report=5 -qopt-report-phase=vec

LOOP BEGIN at <path>/departure_point_eta_mod.F90(253,9)

remark #15305: vectorization support: vector length 4 remark #15309: vectorization support: normalized vectorization overhead 0.303 remark #15300: LOOP WAS VECTORIZED remark #15476: scalar cost: 413 remark #15477: vector cost: 107.250 remark #15478: estimated potential speedup: 3.690 remark #15482: vectorized math library calls: 2 LOOP END



Time measurements for departure_point_eta_mod loops

 $T = \left(\sum_{i=0}^{479} t_i\right) / 480 - \text{average time taken by MPI process}$

 t_i – total time for all 8 loops taken by MPI process with rank #*i* (the job is run on 480 MPI processes)

Compilation options for departure_point_eta_mod.F90

Cray compiler: -hcpu=haswell -03 -hvector3 -hscalar3 -hfp4 -hcache3 -haggress -hnocontiguous -hconcurrent -hflex_mp=default



Time measurements for departure_point_eta_mod loops (cont #2)

Intel compiler

STANDARD

-align array64byte -qopenmp -03 -fp-model precise -xavx (1)

FAST_TRANS

(1) "+" -fast-transcendentals -fimf-precision=high (2)

FAST_TRANS+AVX2

(2) with replacement -xavx => -xCORE-AVX2 (3)



Time measurements for departure_point_eta_mod loops (cont #3)

Cray	Intel		
	STANDARD	FAST_TRANS	FAST_TRANS+AVX2
49.7 sec	63.1 sec	29.8 sec	28.4 sec

Conclusions:

- usage of -fast-transcendentals -fimf-precision=high reduces the elapsed time by over 2 times
- the shortest elapsed time with the Intel compiler is 1.75 times better than with the Cray compiler
- minor speed up from AVX2



Usage of MKL in UM

Frequently called transcendental functions in the UM sources are managed by the following procedure:

```
SUBROUTINE exp_v(n,x,y)
. . .
#if defined(MKL)
CALL vdexp(n, x, y)
#else
DO i=1, n
    y(i) = EXP(x(i))
END DO
#endif
END SUBROUTINE exp_v
```

Similar routines are available in UM for EXP, SQRT, LOG, SIN, COS, ASIN, ACOS, ...



Performance results with Intel compiler

Build #1: STANDARD optimised build

Build #2: FAST_TRANS build for all model files

Build #3: FAST_TRANS build for all model files "+" pre-processor options are set to use the MKL library (-DMKL)

STANDARD	FAST_TRANS	FAST_TRANS + MKL
918 sec	874 sec	877 sec

Conclusions:

- fast-transcendentals provide a reduction in the elapsed time for the job by ~5% with a relatively minor effort
- MKL has no additional benefit



Performance results comparison for Intel and Cray compilers

Using the same run environment

Intel compiler => 874 sec

Cray compiler => 952 sec

with Cray compiler options set at the Met Office with enabled inter-procedural optimisation

Conclusion:

 elapsed time with the Intel compiler is 9% better than with the Cray compiler



Conclusions

- Intel compiler
 - using fast-transcendentals and MKL library
 - vectorisation of some loops is improved
 - o relatively good performance gains can be achieved
 - factor of 2 speed-up for SL departure point calculations loops
 - 5% improvement for full model
 - o relatively minor effort required
- Cray compiler
 - at this stage it is not clear on whether a similar performance benefits are achievable with the compiler



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THANK

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